

## Tutorial 1

**Exercise 1:** For each of the following languages, give an example of 5 words belonging to the language, and an example of 5 words that do not belong to the language.

- a)  $L_1 = \{w \in \{0, 1\}^* \mid \text{the length of word } w \text{ is less than } 5\}$
- b)  $L_2 = \{w \in \{a, b\}^* \mid \text{the number of occurrences of symbol } b \text{ in word } w \text{ is even}\}$
- c)  $L_3 = \{w \in \{0, 1\}^* \mid \text{in } w \text{ is every } 0 \text{ (directly) followed by } 1\}$
- d)  $L_4 = \{w \in \{0, 1\}^* \mid w \text{ begins and ends with the same symbol}\}$
- e)  $L_5 = \{w \in \{a, b\}^* \mid w \text{ contains as a subword the sequence } abb\}$

**Exercise 2:** Let us assume  $\Sigma = \{a, b\}$  and  $n \in \mathbb{N}$ .

- a) How many words in  $\Sigma^*$  are of length  $n$ ?
- b) How many words in  $\Sigma^*$  are of length at most  $n$ ?

**Exercise 3:** For each of the following languages, construct a DFA accepting the given language. Represent the constructed automata by graphs and tables.

- a)  $L_1 = \{w \in \{a, b\}^* \mid w = a\}$
- b)  $L_2 = \{b, ab\}$
- c)  $L_3 = \{w \in \{a, b\}^* \mid \exists n \in \mathbb{N} : w = a^n\}$
- d)  $L_4 = \{w \in \{a, b, c\}^* \mid |w|_a \geq 1\}$
- e)  $L_5 = \{w \in \{0, 1\}^* \mid w \text{ contains subword } 011\}$
- f)  $L_6 = \{w \in \{a, b, c\}^* \mid |w| > 0 \wedge |w|_a = 0\}$
- g)  $L_7 = \{w \in \{a, b\}^* \mid |w| \geq 2 \text{ and the last two symbols of } w \text{ are not the same}\}$
- h)  $L_8 = \{w \in \{a, b\}^* \mid |w|_a \bmod 3 = 1\}$

**Exercise 4:** Construct DFA accepting words beginning with  $abaab$ , ending with  $abaab$ , and containing  $abaab$ , i.e., construct deterministic finite automata accepting the following three languages:

- a)  $L_1 = \{abaabw \mid w \in \{a, b\}^*\}$
- b)  $L_2 = \{wabaab \mid w \in \{a, b\}^*\}$
- c)  $L_3 = \{w_1abaabw_2 \mid w_1, w_2 \in \{a, b\}^*\}$

**Exercise 5:** Describe how to find out for a given DFA  $A = (Q, \Sigma, \delta, q_0, F)$  if:

- a)  $L(A) = \emptyset$
- b)  $L(A) = \Sigma^*$

**\*Exercise 6:** Construct a deterministic finite automaton accepting exactly those words over the alphabet  $\{a, b, c, d\}$  that do not start with  $a$ , do not have  $b$  on the second position, do not have  $c$  on the third position, and do not have  $d$  on the fourth position. (Including those  $w$  where  $|w| < 4$ .)

**\*Exercise 7:** Construct a deterministic finite automaton accepting exactly those words over the alphabet  $\{a, b, c, d\}$  that do not start with  $a$ , or do not have  $b$  on the second position, or do not have  $c$  on the third position, or do not have  $d$  on the fourth position.