

## Tutorial 1

### Exercise 1

What are all the possible values that can be stored in the variable  $x$  after the execution of the following parallel program?

$$x := 10; ((x := x * 2; x := x - 11; x := x + 2) \parallel x := x - 5)$$

### Exercise 2

Let  $R$  be a binary relation on a set  $A$ . Let us define the binary relation

$$E \stackrel{\text{def}}{=} \{(x, x) \mid x \in A\}.$$

It is trivially true that  $R \cup E$  is a reflexive relation.

- Argue that  $R \cup E$  is a reflexive closure of  $R$ .

### Exercise 3

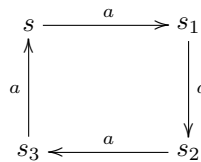
Let  $R$  be a binary relation on a set  $A$ . Let us define the binary relation

$$R^{-1} \stackrel{\text{def}}{=} \{(y, x) \mid (x, y) \in R\}.$$

- Argue that  $R \cup R^{-1}$  is a symmetric relation.
- Argue that  $R \cup R^{-1}$  is a symmetric closure of  $R$ .

### Exercise 4\*

Let us consider the following labelled transition system.



- Define the labelled transition system as a triple  $(Proc, Act, \{\xrightarrow{a} \mid a \in Act\})$ .
- What is the reflexive closure of the binary relation  $\xrightarrow{a}?$  (A drawing is fine.)
- What is the symmetric closure of the binary relation  $\xrightarrow{a}?$  (A drawing is fine.)
- What is the transitive closure of the binary relation  $\xrightarrow{a}?$  (A drawing is fine.)

### Example 5

Let us consider the following CCS definition of a coffee machine.

$$CM \stackrel{\text{def}}{=} \overline{coin}.coffee.CM$$

- Give a CCS process which describes a coffee machine that may behave like  $CM$  but may also steal the money it receives and fail at any time.

**Example 6**

Assume a given labelled transition system  $T = (Proc, Act, \{\xrightarrow{a} \mid a \in Act\})$  such that the sets  $Proc$  and  $Act$  are finite.

- Does it imply that  $\xrightarrow{a}$  is also a finite set? Why?
- Draw an example of an LTS with four states and two actions.
- How can your example be described by a sequential fragment of CCS (with Nil, action prefixing, nondeterminism and recursive definitions of names)?
- Show that in general any finite LTS  $T$  can be described by using only a sequential fragment of CCS.