

**Property modifiers**

Property modifiers are functions of type  $((\text{ot})_{\tau\text{ot}}(\text{ot})_{\tau\text{ot}})$ ; they associate a given root property with a new, modified property.

Here is the basic taxonomy of property modifiers.

*Intersective.* “If  $a$  is a *round* peg, then  $a$  is round and  $a$  is a peg”.

$$[[M_i P]_{wt} a] \models [M^*_{wt} a] \wedge [P_{wt} a].$$

$$\forall w \forall t [[M_i P]_{wt} = [M^*_{wt} \cap P_{wt}]]$$

Necessarily, i.e. in all worlds and times, the set of round pegs equals to the intersection of the sets of round objects and pegs.

*Subsective.* “If  $a$  is a *skilful* surgeon, then  $a$  is a surgeon.”

$$[[M_s P]_{wt} a] \models [P_{wt} a].$$

$$\forall w \forall t [[M_s P]_{wt} \subseteq P_{wt}]$$

Necessarily, i.e. in all worlds and times, the set of skillful surgeons is a subset of the set of surgeons.

*Privative.* “If  $a$  is a *forged* banknote, then  $a$  is not a banknote”.

$$[[M_p P]_{wt} a] \models \neg [P_{wt} a].$$

$$\forall w \forall t [[[M_p P]_{wt} \cap P_{wt}] = \emptyset]$$

Necessarily, i.e. in all worlds and times, the intersection of the set of forged banknotes and banknotes is empty.

**Analyse** the following arguments and decide (prove) which of them are valid:

A<sub>1</sub> *a is a round peg.*  
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*a is round and a is a peg.*

*Jumbo is a small elephant.*  
*Mickey is a large mouse.*  
 -----  
*Jumbo is small and Mickey is large*

*Small things are smaller than large things*  
*Jumbo is small and Mickey is large*  
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*Jumbo is smaller than Mickey*

*Custom officers collected three forged passports*  
*Custom officers collected five forged banknotes*

A<sub>3</sub>

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*Custom officers collected eight forged things*